

# General Certificate of Education June 2010 

Mathematics
MFP2

Further Pure 2

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## Key to mark scheme and abbreviations used in marking

| M | mark is for method |  |  |
| :---: | :---: | :---: | :---: |
| m or dM | mark is dependent on one or more M marks and is for method |  |  |
| A | mark is dependent on M or m marks and is for accuracy |  |  |
| B | mark is independent of M or m marks and is for method and accuracy |  |  |
|  | mark is for explanation |  |  |
| $\checkmark$ or ft or F | follow through from previous incorrect result | MC | mis-copy |
| CAO | correct answer only | MR | mis-read |
| CSO | correct solution only | RA | required accuracy |
| AWFW | anything which falls within | FW | further work |
| AWRT | anything which rounds to | ISW | ignore subsequent work |
| ACF | any correct form | FIW | from incorrect work |
| AG | answer given | BOD | given benefit of doubt |
| SC | special case | WR | work replaced by candidate |
| OE | or equivalent | FB | formulae book |
| A2,1 | 2 or 1 (or 0 ) accuracy marks | NOS | not on scheme |
| $-x$ EE | deduct $x$ marks for each error | G | graph |
| NMS | no method shown | c | candidate |
| PI | possibly implied | sf | significant figure(s) |
| SCA | substantially correct approach | dp | decimal place(s) |

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

MFP2


MFP2 (cont)


MFP2 (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 5(a)(i) | Divide $\cosh ^{2} t-\sinh ^{2} t=1$ by $\cosh ^{2} t$ | M1 |  | $\text { Or } \frac{\sinh ^{2} t}{\cosh ^{2} t}+\frac{1}{\cosh ^{2} t}$ |
|  | Rearrange | A1 | 2 | AG If solved back to front with no conclusion ending $\cosh ^{2} t-\sinh ^{2} t=1$ B1 only |
| (ii) | $\frac{\mathrm{d}}{\mathrm{~d} t}\left(\frac{\sinh t}{\cosh t}\right)=\frac{\cosh ^{2} t-\sinh ^{2} t}{\cosh ^{2} t}$ | M1A1 |  |  |
|  | $=\operatorname{sech}^{2} t$ | A1 | 3 | AG |
| (iii) | $\frac{\mathrm{d}}{\mathrm{~d} t}(\operatorname{sech} t)=-(\cosh t)^{-2} \sinh t$ | M1A1 |  | Allow A1 if negative sign missing |
|  | $=-\operatorname{sech} t \tanh t$ | A1 | 3 | AG |
| (b)(i) | $\left(\frac{\mathrm{d} x}{\mathrm{~d} t}\right)^{2}+\left(\frac{\mathrm{d} y}{\mathrm{~d} t}\right)^{2}=\operatorname{sech}^{4} t+\operatorname{sech}^{2} t \tanh ^{2} t$ | M1 |  | Allow slips of sign before squaring for this M1 |
|  | Use of $\tanh ^{2} t+\operatorname{sech}^{2} t=1$ | m1 |  | Correct formula only for m1 |
|  | $=\operatorname{sech}^{2} t$ | A1 |  |  |
|  | $\therefore s=\int_{0}^{\frac{1}{2} \ln 3} \operatorname{sech} t \mathrm{~d} t$ | A1 | 4 | AG (including limits) |
| (ii) | $u=\mathrm{e}^{t} \quad \mathrm{~d} u=\mathrm{e}^{t} \mathrm{~d} t$ | B1 |  |  |
|  | $\int \operatorname{sech} t \mathrm{~d} t=\int \frac{2}{u^{2}+1} \mathrm{~d} u$ | M1A1 |  | CAO M1 for putting integrand in terms of $u \quad$ (no $\operatorname{sech}(\ln u)$ ) |
|  | $\left[2 \tan ^{-1} u\right]$ | A1 |  | Or $2 \tan ^{-1} e^{t}$ |
|  | Change limits correctly or change back | m1 |  | At some stage |
|  | $=\frac{2 \pi}{3}-\frac{2 \pi}{4}=\frac{\pi}{6}$ | A1 | 6 | CAO |
|  | Total |  | 18 |  |
| 6(a) | $\frac{1}{(k+2)!}=\frac{k+3}{(k+3)!}$ |  |  |  |
|  | Result | A1 | 2 |  |
| (b) | Assume true for $n=k$ <br> For $n=k+1$ |  |  |  |
|  | $\sum_{r=1}^{k+1} \frac{r \times 2^{r}}{(r+2)!}=1-\frac{2^{k+1}}{(k+2)!}+\frac{(k+1) 2^{k+1}}{(k+3)!}$ | M1A1 |  | If no LHS of equation, M1A0 |
|  | $=1-2^{k+1}\left(\frac{1}{(k+2)!}-\frac{k+1}{(k+3)!}\right)$ | m1 |  | m 1 for a suitable combination clearly shown |
|  | $=1-\frac{2^{k+2}}{(k+3)!}$ | A1 |  | clearly shown or stated true for $n=k+1$ |
|  | True for $n=1$ <br> Method of induction set out properly | $\begin{aligned} & \text { B1 } \\ & \text { E1 } \\ & \hline \end{aligned}$ | 6 | Shown <br> Provided previous 5 marks all earned |
|  | Total |  | 8 |  |

MFP2 (cont)


